Role of V-V dimers on structural, electronic, magnetic, and vibrational properties of VO$_2$ by first-principles simulations and Raman spectroscopic analysis


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We investigate the vibrational properties of VO$_2$, particularly the low-temperature M1 phase by first-principles calculations using the density functional theory as well as Raman spectroscopy. In the theoretical aspect, the phonon calculation requires structure optimization and force calculations on a large supercell to obtain an accurate result, and strong correlation effects in VO$_2$ make this task very challenging. We perform the structural optimization using SCAN meta-GGA functional and obtain the optimized crystal structures with the correct energy hierarchy as well as correct electronic properties for the rutile and M1 phases of VO$_2$ including both the nonmagnetic (NM) and antiferromagnetic (AFM) spin ordering. We show both the NM-M$_1$ and AFM-M$_1$ are insulators, whereas NM-R and AFM-R are metals. However, FM-R and FM-M$_1$ are found be same as energetically favorable and becomes half-metal. Based on the harmonic approximation around the optimized structures obtained from the NM calculations at zero temperature, we reproduce the phonon softening in the rutile phase as well as the phonon stiffening in the M$_1$ phase. Our phonon calculations reveal that both the NM-M$_1$ phase and AFM-M$_1$ are dynamically stable, whereas FM-M$_1$ is found to be dynamically unstable. In addition, we perform Raman experiment on VO$_2$ thin films which stimulate enormous interests in the field of thin-film engineering for transition metal oxides. We demonstrate from the comparison between theoretical calculations and Raman measurements that the subtle change of the V-V dimer due to the strain effect can be reliably detected by the Raman spectroscopy, which could be a new framework to determine the subtle change of crystal structure for transition metal oxide thin films.

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I. INTRODUCTION

Vanadium oxide (VO$_2$) has been a focus of intense research since its discovery in 1959 [1]. Besides academic interest, it underpins a plethora of applications including gas sensors [2], window coatings [3], resistive random access memory (RRAM) devices [4], electronic switches [5–7], and so on. The versatile phase diagram of VO$_2$ showcase well known first order metal-insulator transition (MIT) at almost room temperature (340 K) and ambient pressure accompanied by a structural transition from a high-temperature and high-symmetry rutile (R phase) to a low-temperature and low-symmetry monoclinic (M$_1$ phase). Due to this intricate concomitant nature of these two transitions, the controversy between predicting the accurate structural properties and accurate electronic properties has not been still completely resolved. Strong electron correlations has been believed to be a key mechanism for explaining large energy gap of 0.7 eV in the insulating M$_1$ phase of VO$_2$ [8–10]. Several other proposals suggest that the electron correlations may not be good enough and the structural properties should be also taken into account in combination with the strong electron correlations effects for more complete description of the VO$_2$[11–13]. Though extensively studied, a consensus for a exact mechanism of MIT in VO$_2$ is still elusive. Overall, extensive research indicate that the role of structural properties can not be underestimated in explaining the rich phase diagram of VO$_2$ [14–16].

The role of defects, vacancies, doping and, strain in this phase diagram has been an ongoing topic of research in recent time [17]. For example, Wickramaratne et al. [18] find that the V Frenkel defects in the insulating phase of VO$_2$ can reduce resistivity compared to pristine VO$_2$. Using diffusion Monte Carlo, Ganesh et al. [19] show that the gap in the M$_1$ phase can be suppressed by doping with the oxygen vacancies. Several investigations suggest that strain can greatly influence the MIT mechanism [20–23]. Therefore, the structural properties should be investigated more carefully and lattice vibrational properties of VO$_2$ can give us a new insight of its structure.
However, achieving an accurate description of the lattice vibrational properties of the VO$_2$ turns out to be a nontrivial task from both the experimental and theoretical point of view. For example, the bottleneck of single-crystal inelastic neutron scattering (INS) is the incoherent vanadium neutron scattering cross-section. Even, some of the existing Raman spectroscopic studies of the structural phase transition (SPT) in epitaxial VO$_2$ films have been found to be inconsistent due to the large thicknesses of studied films (80–100 nm) or even misinterpreted due to the strong signals from the substrate [24–27]. Besides these experimental challenges, achieving an exact theoretical description of the lattice dynamics of VO$_2$ has been a tougher nut to crack. Since lattice vibrational properties are strongly related with the structure of the material, first-principles-based methods that take into account the much needed material specific information can be an ideal tool for this task. However, a reliable exchange functional which can correctly describe the vibrational properties of all the phases of VO$_2$ is not readily available and still an going topic of research. It has been found that the standard functional such as local density approximation (LDA) and generalized gradient approximations (GGA) can not describe the structural, electronic and magnetic features of the R and M$_1$ phases simultaneously [15, 28]. Thus, the LDA and GGA-based calculations clearly manifest the well known “band gap” problem in DFT.

To ameliorate this “band gap” issue, several attempts have been already made to go beyond the LDA or GGA functional. For example, the modified Becke-Johnson (mBJ) exchange potential has been demonstrated to be very efficient for describing the MIT in VO$_2$ [28]. The GW method and its variants successfully predict the electronic feature of the MIT [29–31]. The dynamical mean-field theory and its cluster extensions correctly describe the electronic properties of both the R and M$_1$ phases of VO$_2$ [11, 32]. Moreover, hybrid functionals efficiently describe the electronic properties of VO$_2$ [33] and is found to be also successful in describing the structural properties of all the phases of VO$_2$ [34]. First-principles-based quantum Monte Carlo-based calculations have been also performed for VO$_2$ [35]. Unfortunately, all these efforts fall short for the phonon calculations of VO$_2$.

For example, the Hellmann–Feynman force calculations are not possible using the mBJ ruling out the possibility of phonon calculations within this exchange approximation. Phonon calculations using the GW formalism has not been formulated yet. Cluster extension of DMFT such as dynamical cluster approximations (DCA) and its typical medium extension named as typical medium DCA (TMDCCA) for disordered phononic systems has been recently developed [36, 37]. Unfortunately, such DCA and TMDCCA method for phononic systems are currently available for parameter-based model calculations. Phonon calculations using hybrid functionals turn out to be not a practical approach due to computational expenses.

Considering all these limitations, the GGA + U method [38–41] has been extensively used for phonon calculations of VO$_2$ because it is claimed to resolve the “band gap” problem and at the same time it is computationally less expensive. However, the GGA + U method remains controversial in producing an accurate description of VO$_2$. Anisimov and coauthors [38] find insulating nature of the R phase which strongly disagree with experimental findings. Mellan et al. [40] predict electronic structure of VO$_2$ that is consistent with experiment using nonspin polarised GGA + U calculations. But, U value within the LDA + U method has been treated so far as a free parameter and the results are also very sensitive with the choice of U value. For example, Budai et al. [41] point out that the U value less than 3.4 eV is more appropriate in determining energy difference between the R and M$_1$ phase that could be more consistent with experiment, but such lower U value can produce more smaller bandgap. Hence, an accurate prediction of the U value rather using it as a free parameter or bare atomic value, may have a paramount importance for reliable estimation of the vibrational properties of VO$_2$. To best of our knowledge, calculations for determining U value of VO$_2$ via the constrained random phase approximation (cRPA) or linear response method are still missing. Another important thing is to include temperature effect and anharmonicity in phonon calculations. Such calculations [41] have been already performed and can help to validate further theoretical development.

Besides the “band gap” problem, another challenge is to predict the correct magnetic structure of VO$_2$. The magnetic ground state of the Mott-Hubbard insulators generally shows antiferromagnetic order. However, VO$_2$ is a prototypical example of strongly correlated system whose magnetic ground state is a spin singlet (nonmagnetic)[NM]. The R phase is experimentally found to be paramagnetic above the transition temperature of 340 K [42, 43]. While the M$_1$ phase is found to be NM [44], the $S = \frac{1}{2}$-Heisenberg chains are believed to characterizing the M$_2$ phase [45].

Cluster DMFT approach does not suffer in predicting the true singlet state. However, it is not practical to use cluster DMFT for large supercells due to computational expenses [11, 13]. On the other hand, the DFT like mean-field theory fails to predict a true singlet state. It can only determine a single-determinant state. Again, several efforts have been made by applying the improved functional to predict the correct magnetic ground state. Eyert [33] claims that the screened hybrid functional can provide a good description of the electronic and magnetic structures of VO$_2$ phases. However, Grau-Crespo et al. [46] do not agree with Eyert’s results [33] and they find a magnetic ground state for the M$_1$ phase, a nonmetallic ground state for the R phase, and an R-M1 energy difference in significant disagreement with the experimental latent heat using hybrid functional in their calculations. Other approach like the LDA + U method also suffers in predicting correct magnetic structure of all the phases of VO$_2$. Mellan et al. [40] show that LDA + U can predict correct electronic and magnetic ground state of VO$_2$ using non-spin-polarized calculations. However, such conclusions do not hold true when spin-polarized calculations are considered. Anisimov et al. [38] predict an antiferromagnetic ground state of the M$_1$ phase using the LDA + U method which is not correct. However, the issue of the hybrid functional considering spins are reexamined by Xu et al. [34] and they point out that the results are sensitive to the nature of the pseudopotentials used in the calculations. For example, they show in Ref. [34] that the AFM-M$_1$ state is metastable if typical oxygen.
pseudopotentials is used but it becomes unstable if hard potential is considered in the calculations. They show that the calculated total energies according to the AFM-R and NM-R phase are higher than FM-R by 125 and 140 meV per formula unit, respectively [34], and thus FM-R is found to be ground state of the R phase which contradicts with experiment. This recent hybrid functional study show the NM-M1 phase is more stable compared to the AFM-M1 phase which is consistent with the experiments [42,43]. Three possible spin configurations, termed as A-AFM, C-AFM and G-AFM are considered to predict the correct antiferromagnetic configurations of the M2 phase using hybrid functional and both A-type and G-type AFM-M2 is found to agree with the experimentally derived model in which M2 is AFM and local magnetic moments exist only on the canted zigzag V-V chains. The Quantum Monte Carlo simulations [35] are also applied to resolve the issue related with spin polarization in the DFT description of VO2.

The accuracy of ab initio electron correlation and electron densities in correctly describing the physics of VO2 have been investigated in detail in Ref. [47]. In this study, among all the nonhybrids, the SCAN functional turns out to be as nearly balanced in terms of magnetization across the M1-R transition. In addition, it also accurately determine the ground state crystal structure of VO2. Indeed, predicting accurate magnetic structure of VO2 including all the phases from band theory is still an open question.

In this paper, we present a comprehensive study of the lattice dynamics and electronic structures using various DFT functionals and benchmark our calculations with experiments. By comparing with Raman spectroscopy, we investigate the interplay between strain effect and local environment (e.g., spectral shifts of the V-V and V-O phonon modes) in epitaxial VO2 thin films deposited on MgF2 (001) and (110) substrates. We show that our calculations are in a good agreement with the observed Raman shifts of the characteristic phonon modes induced by the epitaxial strains imposed on VO2 thin films. Our work demonstrates that Raman spectroscopy could serve as a reliable way to detect the subtle change of V-V dimer in the strained VO2.

We have organized this paper as follows: we give details of our first-principles simulations in Sec. II. We provide information of our experimental set up in Sec. III. We present and discuss our results in Sec. IV. Finally, we conclude our discussions in Sec. V.

II. COMPUTATIONAL DETAILS

We consider a plane-wave basis and the projector-augmented-wave (PAW) method as implemented in the Vienna Ab initio Simulation Package (VASP) [49,50]. We have used several different exchange correlation functional including the LDA, the PBE GGA [51], and the SCAN [52]. We note that the SCAN has been implemented for self-consistent calculations in the VASP and such self-consistent implementation is still not available in other first-principles packages like WIEN2K. We choose PBE GGA pseudopotential in our calculations using SCAN. For electronic structure calculations, we use the plane-wave cutoff energy as 500 eV. We also verify that there is no appreciable changes in the results using a cutoff energy of 600 eV. For all Brillouin-zone sampling, \( \Gamma \)-centered k-point grids is considered as \( 16 \times 16 \times 16 \). The self-consistent calculations are considered to be converged by considering \( 10^{-4} \) eV between successive iterations, and the convergence of structural relaxation is decided by the total energy difference between two successive ionic steps as \( 10^{-3} \) eV. We have also cross-checked our electronic structure calculations by using mBJ calculations as available in WIEN2K. The results obtained from the WIEN2K are not shown here. For the phonon calculations, we have employed the pseudopotential band method and the supercell approach that are implemented in VASP [49,50] and PHONOPY [53]. As a standard supercell-based phonon calculations, force-constants are computed by means of the Hellmann-Feynman theorem [54].

III. EXPERIMENTAL DETAILS

High-quality 10-nm-thick VO2 films were grown on rutile MgF2 (001) and (110) single crystal substrates by reactive molecular-beam epitaxy (MBE) via codeposition method under a distilled ozone background pressure at the PARADIM Thin Film Growth Facility at Cornell university [55]. Raman microscopy analysis was conducted at the Center for Nanoscale Materials at the Argonne National Laboratory. The spectra were recorded using a Raman microscope (inVia Reflex, Renishaw, Inc.) with spectral resolution of 0.5 cm\(^{-1}\) using 532 nm excitation from a diode pumped solid state laser (RL532CS0, Renishaw, Inc.). Samples were held in a nitrogen-purged temperature-controlled stage (THMS600/TMS94/LNP94, Linkam Scientific Instruments Ltd). Excitation and collection of scattered light occurred through a 50\(\times\) objective (Leica, NA=0.50). The laser power was set to 0.64 mW to exclude local heating effect. Collected spectra are typically consisted of the average of 20 integrations, where each integration was collected for 1 min.

IV. RESULTS AND DISCUSSIONS

We begin our discussions by investigating the structural properties of VO2. The well-known experimental crystal structure of VO2 [48] as described in Fig. 1. The unit cell contains 6 atoms for the R phase and 12 atoms for the M1 phase in our considered experimental structure. As shown in Fig. 1(a), the V-V atoms form a periodic V chain with fixed V-V bond distance as 2.86 Å in the rutile structure, whereas there are significance differences in the arrangement of the V atoms along the rutile \( C_R \) axis in the M1 phase, as demonstrated in Fig. 1(b). In this M1 phase, the V atoms are arranged such a way that they form dimmer alternatively and tilt along the \( C_R \) axis, which leads to doubling of the unit cell volume of that for the R phase with V-V distance as 2.62 Å (bonding) and 3.16 Å (antibonding). With this understanding of available experimental crystal structure, we perform structure optimization of both the R and M1 phases of VO2.

For structure optimization, we consider the optimization process, in which both the lattice parameters and atoms are allowed to move for searching the minimum energy configurations. First, we optimize the crystal structure of the R phase using different functionals without considering any spin
ordering (see Fig. 2) and compare it with experimental data [48] (see Fig. 1) and previously reported values [34] presented in Table I. For SCAN meta-GGA functional, the V-V pair distance changes from the experimental value 2.86 Å to 2.76 Å, whereas it is 2.77 Å for the GGA functional. We note that there is no significant changes in the results obtained from the SCAN meta-GGA and GGA functional. However, this is certainly not true for the case of M₁ phase excluding any spin ordering. Our calculations suggest that the optimization process is extremely sensitive to the functional used in the calculations as summarized in Table II. We find that the LDA functional completely fails to optimize the M₁ structure. We observe that the long V-V dimer and short V-V dimer distance becomes almost equal as 2.72 Å which imply that the M₁ structure reduces to the rutile like structure through the LDA optimization process. Hence, like electronic properties, our calculations reveal that the LDA is not applicable to determine the structural properties of the M₁ phase. The convergence of our LDA calculations have been carefully tested as discussed in Appendix A. However, the situation becomes better when the GGA is applied in our calculations. In the optimized M₁ structure based on the GGA functional, the long V-V dimer distance decreases to 3.0 Å from the experimental value 3.16 Å and short V-V dimer separation decreases to 2.59 Å from the experimental value 2.62 Å. Such drastic change in the dimer distance clearly indicates that the M₁ structure again tends to go to the rutile phase through the optimization process. As has been already found [34], this failure of the LDA and GGA can be cured by the hybrid functional. To overcome this barrier, we have utilized SCAN meta-GGA functional for optimizing the M₁ structure. As summarized in Table II, in the SCAN optimized M₁ structure, the long V-V dimer nature survive as 3.16 Å which is very close to the value 3.14 Å as found in hybrid calculations [34] and exact as 3.16 Å as found in experiment [48]. The short V-V dimer using SCAN functional is found to be 2.47 Å which is also to 2.44 Å as found from the hybrid functional calculations. Thus, like hybrid functional, the optimized crystal structure using SCAN has all the expected features of the experimentally derived structure: All V-V chains of M₁ are found to be dimerized and canted along the rutile axis, whereas all V-V chains form straight undimerized one in the rutile phase. In addition, we have also performed structure optimization of both the rutile and M₁ phases of VO₂ including ferromagnetic (FM) and antiferromagnetic (AFM) spin ordering. The optimized FM-R and FM-M₁ are presented in Fig. 3. In the FM-M₁ optimized structure, the long V-V dimer distance deviates from the experimental value 3.16 Å to 2.93 Å, whereas the short V-V

**TABLE I.** Optimized V-V distance for the rutile phase of VO₂ obtained from our calculations using different functional and spin ordering.

<table>
<thead>
<tr>
<th>Functional</th>
<th>V-V distance</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exp. [48]</td>
<td>2.86</td>
</tr>
<tr>
<td>GGA (NM)</td>
<td>2.76</td>
</tr>
<tr>
<td>Ref. [34] (NM)</td>
<td>2.80</td>
</tr>
<tr>
<td>SCAN (NM)</td>
<td>2.77</td>
</tr>
<tr>
<td>SCAN (FM)</td>
<td>2.83</td>
</tr>
<tr>
<td>SCAN (AFM)</td>
<td>2.82</td>
</tr>
</tbody>
</table>

**TABLE II.** Optimized long and short V-V dimer distances for the M₁ phase of VO₂ obtained from our calculations using different functional and spin ordering.

<table>
<thead>
<tr>
<th>Functional</th>
<th>V-V dimer (long)</th>
<th>V-V dimer (short)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exp. [48]</td>
<td>3.16</td>
<td>2.62</td>
</tr>
<tr>
<td>LDA (NM)</td>
<td>2.72</td>
<td>2.72</td>
</tr>
<tr>
<td>GGA (NM)</td>
<td>3.0</td>
<td>2.59</td>
</tr>
<tr>
<td>Ref. [34] (NM)</td>
<td>3.14</td>
<td>2.44</td>
</tr>
<tr>
<td>SCAN (NM)</td>
<td>3.16</td>
<td>2.47</td>
</tr>
<tr>
<td>SCAN (FM)</td>
<td>2.93</td>
<td>2.73</td>
</tr>
<tr>
<td>Hybrid (FM) [34]</td>
<td>2.94</td>
<td>2.69</td>
</tr>
<tr>
<td>SCAN (AFM)</td>
<td>3.07</td>
<td>2.80</td>
</tr>
</tbody>
</table>
dimer distance becomes 2.73 Å from the experimental value 2.62 Å. As a result, the differences between the long and short V-V dimer distances deviates significantly in compare to the experimental value 0.69 Å to 0.2 Å. Therefore, in the optimized FM-M1 VO$_2$, the corresponding structure tends to lose its dimer character. The obtained optimized structure of M1 phase using the SCAN functional is in agreement with the previous Hybrid-functional calculations [34]. As we discussed in the SCAN predicted optimized structure, the long dimer value is found to be 2.93 Å which is very close to a value of 2.94 Å obtained from the Hybrid functional calculations. The predicted short dimer distance value is found to be 2.73 Å which is also close to the Hybrid functional predicted value as 2.69 Å. Thus, as discussed in the previous hybrid functional calculations, we also observe that the optimized FM-M1 tends to reduce to the FM-R phase and survive in a new monoclinic phase with crystal structure in between M1 and R which is named as M0 state. This M0 state is believed to be ferromagnetic in nature. Existing experimental data [56,57] at liquid-helium temperature also suggest possibility of such a phase. In the R-FM VO$_2$ the distance between V-V atoms becomes 2.83 Å from the experimental value 2.86 Å. However, in the AFM-M1 optimized structures (see Fig. 4), the difference between the long V-V dimer and short V-V dimers remain more close to the experimental value compared to the FM-M1 structure. In the AFM-M1, the long V-V dimer value reduces to 3.07 Å from the experimental value 3.16 Å, whereas the short V-V dimer value becomes 2.82 Å from the experimental value 2.62 Å. So, the difference between long and short V-V dimer becomes 0.27 Å from the experimental value 0.69 Å. The V-V atom distance is found to be 2.82 Å in the optimized structure of AFM-R phase.

Structure optimizations of both the rutile and M1 phases lead us to search for the energetically favorable phase of VO$_2$. Our non-spin-polarized calculations show that the low-temperature M1 phase is energetically lowered than the high-temperature rutile phase by 22.18 meV per atom. In our antiferromagnetic (AFM) calculations, energy of the M1 phase is found to be lower from the energy of the rutile phase by 27.92 meV per atom. The energy of the FM-R is found to be almost the same as the AFM-M1. In particular, the energy of the FM-M1 is found to be higher compared to the FM-R phase by very small value as 1 meV per atom which is not sufficient to conclude that the FM-M1 is not energetically favorable compared to the FM-R phase due to the numerical precision of DFT.

Next, we study the electronic properties of the M1 phase focusing on the effect of the structural optimization on the electronic structure, to draw an accurate band theory picture of the M1 phase. Fig. 5 presents the electronic density of states (DOS) based on our optimized structures. To treat the comparison on equal footing, we use SCAN functional in the calculation of electronic DOS from the structures that are obtained from different functional. As shown in the top panel of Fig. 5, there is no gap in the DOS corresponding to the LDA optimized structure. However, a pseudogap feature tends to emerge in the DOS of the GGA optimized structure as shown in the middle panel of the Fig. 5. Such small gap in the DOS with the GGA optimized structure was also previously reported and our calculations are consistent with these previous calculations [39,41]. Interestingly, we find a fully gapped spectrum with the SCAN optimized structure as displayed in the bottom panel of Fig. 5.

Figure 6 displays the variation of the density of states as a function of various values of short V-V dimer separation. As it is clearly seen from the top to bottom of this figure, there is no gap in the density of states for the V-V dimer distance as 2.59 Å. Interestingly, a finite gap emerges as the V-V dimer separation is varied from 2.59 Å to 2.48 Å. Thus, our calculations suggest that a gap can be opened up for the M1 phase depending only on the structure property without considering any Hubbard onsite coulomb interactions. From our calculations, it is certainly clear that the role of Peierl's distortion cannot be neglected in determining the insulating nature of the M1 phase. Such observations
strongly suggest that the M$_1$ phase is not a conventional Mott insulator.

The next question we address here concerns the validity of the SCAN functional in describing the electronic properties of both the rutile and M$_1$ phases of VO$_2$, based on the obtained optimized structure. The calculated density of states considering various spin orderings are presented in Fig. 7. From the optimized structure considering nonmagnetic (NM) state, SCAN-based non-spin-polarized calculations predict the high temperature rutile phase as a metal and the low-temperature M$_1$ phase as an insulator [see Figs. 7(a) and 7(b)]. These findings are consistent with experiments. We note that previous calculations based on different functional fail to correctly describe both the phases of VO$_2$ simultaneously. For example, the LDA + U method find insulating nature of the rutile phase of VO$_2$ [38,58]. However, mBJ and hybrid functional as we discussed before can successfully describe both VO$_2$ phases. As we have already mentioned, mBJ cannot be utilized for calculating the forces and hybrid functional is computationally very expensive. Hence, they are not highly suitable particularly for phonon calculations of VO$_2$. In addition to nonmagnetic calculations, we have also performed spin-polarized calculations for computing the electronic properties of both the rutile and M$_1$ phases of VO$_2$. As shown in Fig. 7(f), we still find the insulating nature of the M$_1$ phase even if including antiferromagnetic spin ordering. Here, we note that previous LDA + U calculations [39] overestimate the band gap by finding the energy gap value as 1.33 eV compared to the experimental value 0.6 eV, whereas our spin-polarized SCAN calculations yield bandgap value as 0.45 eV. At the same time, we also find the gapless metallic behavior of the rutile phase including the same AFM ordering [Fig. 7(e)]. However, our calculations using SCAN functional find both the rutile and M$_1$ phase as a half-metal for ferromagnetic spin ordering [Figs. 7(c) and 7(d)]. The obtained half-metallic nature instead of insulating of the FM-M$_1$ phase can be understood from the large variations of the V-V dimer in the optimized structure.
FIG. 7. Electronic density of states (DOS) for high-temperature rutile (R) and low-temperature monoclinic (M1) phases of VO₂ obtained using SCAN meta-GGA functional considering both the non-spin-polarized and spin-polarized calculations. In spin-polarized calculations, ferromagnetic (FM) and antiferromagnetic spin orderings are included.

Finally, we discuss the vibrational properties of both the rutile and M₁ phases of VO₂. Figure 8 shows the phonon dispersion curves of R-VO₂ using SCAN meta-GGA functional without including spin ordering. We have also performed same calculations using GGA functional. We find that the phonon dispersion for the rutile phase using the SCAN does not deviate significantly from the results using the GGA functional and observe the phonon softening instabilities in both the SCAN and GGA calculations. We consider the soft phonon modes are the unstable phonons whose frequencies are imaginary or negative. To identify which phonon modes are softening, we look into the partial phonon density of states of the rutile phase. As shown in Fig. 9, the soft phonon modes are mainly originated from the V atoms.

FIG. 9. Partial phonon density of states of the R-VO₂ calculated using the SCAN meta-GGA functional within the zero temperature and harmonic approximation. The low-frequency soft modes are mainly contributed by the V atoms.

FIG. 8. Phonon dispersions of the R-VO₂ calculated using the SCAN meta-GGA functional within the zero temperature and harmonic approximation. Observe the phonon softening instability of the R phase at \( q = \Gamma, M, X \).
FIG. 10. The phonon density of states (PDOS) of the R-VO$_2$ obtained from zero temperature harmonic approximation-based calculations. Our computed PDOS for the R-VO$_2$ is in agreement with neutron scattering data [41].

We also observe that our calculations are able to capture some features of the spectra that agree better with the experimental spectrum compared to previous theoretical calculations [41]. For example, the peak around 55 meV corresponding to the experimental DOS is shifted to around 65 meV in the DOS obtained from the previous calculations [41]. Also, previous calculations find DOS at the high-energy region remain around 83 meV, whereas the bandwidth of the experimental spectrum is larger. We note that the bandwidth of our calculated spectrum is much closer to the band width of the experimental DOS compared to previous finite temperature calculations. Although the high temperature rutile phase is believed to be anharmonic, the low-temperature M$_1$ phase is found to be highly harmonic. So, we expect our theoretical framework is more suitable for the M$_1$ phase, which is our next topic of discussion.

We have computed phonon dispersion of the M$_1$ phase based on the non-spin-polarized calculations as displayed in Fig. 11. The calculated dispersion curve for the M$_1$ phase is in good agreement with previous calculations [66]. As shown in Fig. 10, unlike rutile phase, there is no phonon softening which is consistent with experimental observations [41]. It confirms that this M$_1$ phase is the stable structure of VO$_2$ at low temperature. Such structural information can be directly probed in Raman spectra. To understand that, a careful analysis of the phonon density of states can be good a starting point.

The phonon density of states of the M$_1$ phase is presented in Fig. 12. Followed by dispersion, there are no negative frequencies in the low-frequency region of our calculated phonon density of states which confirm the stability of the M$_1$ phase. Such dynamical stability for the AFM-M$_1$ phase is also predicted (see Appendix B). We compare our calculated phonon density of states at $T=0$ K with the phonon density states corresponding to $T=298$ K obtained from experiment using neutron spectrometer as reported in Ref. [41]. We find our zero temperature calculations using SCAN functional successfully capture the experimentally observed phonon density of states at room temperature. To check the performance of SCAN against other functional, we also compare our results with

FIG. 11. Phonon dispersions of the M$_1$-VO$_2$ calculated using the SCAN meta-GGA functional within the zero temperature and harmonic approximation. The absence of any negative phonon frequencies (imaginary frequencies) suggesting the stability of the M$_1$ structure at low temperature.

FIG. 12. The phonon density of states of the M$_1$-VO$_2$ obtained from zero temperature harmonic approximation-based calculations. Our computed PDOS of the M$_1$-VO$_2$ is in excellent agreement with the neutron scattering data [41].
FIG. 13. Comparison of the phonon density of states of the M1 phase of VO$_2$ obtained from the experimental structure (top) and the optimized structure (bottom). In both calculations, SCAN meta-GGA functional has been used. In the optimized structure, there is no negative frequency showing stability of the structure, however, the peak position deviates from the positions as found in Raman spectra. However, this agreement can be improved by considering experimental structure. But, there will be negative frequency associated with the phonon density of states if phonon calculations are done with out optimizing the experimental structure as expected.

previous LDA + U calculations [41] as shown in the lower panel of Fig. 12. Comparison between the results obtained from SCAN and LDA + U clearly shows that the results obtained from SCAN serves better than the LDA + U. In particular, the peak features in the low-frequency region around 20 meV is more intense compared to the LDA + U results as observed in experiments.

We take a more closer look on the phonon density of states and study the effect of the V-V dimer on it. The role of V-V dimerization on the insulating behavior of the M1 phase is well understood now, whereas its effect on the lattice vibrations is still not extensively studied. Here, we aim to explore such physics. As we have already discussed that the V-V dimer distance deviates significantly from the experimental one, we compare phonon density of states of M1 phase using both optimized and experimental structure as shown in Fig. 13. We observe that there are large number of negative frequencies in the low-frequency region of the phonon density of states derived from experimental structure as displayed in upper panel of Fig. 13, whereas there are no such negative frequencies in the low-frequency region of the phonon density of states considering optimized structure as shown in the lower panel of Fig. 13. The absence of such negative frequencies in the low-frequency region of the phonon density of states corresponding to optimized structure is well expected. Moreover, there are also other noticeable differences. There is a peak in the low-frequency region around 190 cm$^{-1}$ and a peak in the high frequency region around 609 cm$^{-1}$ in the phonon density of states obtained from with out optimizing the structure. The low-frequency peak is mainly contributed from V-V pair and high frequency peak is originated from V-O pair which can be understood from Fig. 14. In addition, we investigate atomic displacement as presented in Fig. 15. To enable a proper comparison with Raman modes, these vibrational eigenvectors correspond to frequencies at the gamma point of two particular regions. Note that the low-frequency atomic displacement is governed by the vanadium dimer vibration while the high frequency eigenvector is a manifestation of oxygen atom displacements only. The positions of the peak and nature of the vibrations are in excellent agreement with the observed Raman spectra. However, the position of the peaks are shifted in the phonon density of states corresponding to optimized structure compared to without optimization one. We attribute this to the drastic change in the short V-V dimer distance that occurred in the optimization process Table II. We also note that peaks in the phonon DOS and Raman spectrum are not directly comparable. The Raman spectrum is only sensitive to zone-center Raman active modes, but the phonon DOS

FIG. 14. Partial phonon density of states for V and O atoms of the M1 phase. The vibrational density of states at the low-frequency region around 190 cm$^{-1}$ is mainly dominated by V atoms. However, at the high frequency region around 609 cm$^{-1}$, there is significant contribution from both the V and O atoms.

FIG. 15. Vibrational eigenvectors (phonon modes) with their corresponding frequency modes at 185.13 cm$^{-1}$ for the left and 612.44 cm$^{-1}$ for the right panel, respectively. The red spheres represent vanadium atoms and green spheres are oxygen. The vectors indicate the atomic displacements for each individual species corresponding to a snapshot of the vibrational movement. Images were generated using Ref. [65].
integrates all phonon modes across the Brillouin zone, with peaks resulting from flat branches or van Hove singularities. Therefore, the meaning of peaks in the Raman spectrum and phonon DOS is different.

Modulation of the V-V dimer length can be accomplished with strain engineering. It has previously been shown in VO$_2$/TiO$_2$ epitaxial thin films that tensile strain on the c$_R$ axis shifts the MIT mechanism toward bulklike characteristics largely driven by the Peierls physics while elongation of the c$_R$ axis induces a larger influence from electron correlation or Mott physics [20–22]. However, due to the strong signal from the TiO$_2$ in Raman spectroscopy, the strain effect on the phonon modes has been misinterpreted [27]. Moreover, although strain has been accomplished on numerous substrates such as ZnO [67], Al$_2$O$_3$ [68], LSAT [69], and RuO$_2$ [70], the formation of rotational domains may complicate fundamental structural analysis in the investigation of the MIT. Like TiO$_2$, MgF$_2$ is isostructural to VO$_2$ in its high temperature phase, and exhibits weaker Raman response than TiO$_2$ substrate [71] and thus we selected it as the substrate for the epitaxial growth of VO$_2$. Fabrication of VO$_2$ on MgF$_2$ (001) induces the tensile strain of the c$_R$ axis, while MgF$_2$ (110) films elongate the c$_R$ axis [20,23]. Indeed, using Raman spectroscopy we observed spectral shift of the characteristic Raman peaks which represent V-V and V-O phonon modes. As shown in the right panels of Figs. 16 and 17, low-frequency peak is shifted from 196 cm$^{-1}$ to 197 cm$^{-1}$, whereas high frequency peak is shifted from 609 to 618 cm$^{-1}$ with the application of strain. Such spectral displacement is shown in our calculated phonon density of states by manipulating V-V dimer. As presented in the left panels of Figs. 16 and 17, the low-frequency peak has been shifted from 190 to 230 cm$^{-1}$ as short dimer V-V distance is varied from 2.62 Å to 2.47 Å. Similarly, the high frequency peak is deviated from 609 to 628 cm$^{-1}$.

V. CONCLUSIONS

In this paper, we have computed structural, electronic and vibrational properties of the R and M$_1$ phases of VO$_2$ using first-principles calculations. We have employed the SCAN meta-GGA functional and successfully optimized the M$_1$ structure. The performance of the SCAN has been compared with various other functional in optimizing the M$_1$ structure. The SCAN optimized structure has been shown to produce consistent electronic properties including both the R and M$_1$ phases of VO$_2$. The low-temperature M$_1$ phase is found to be energetically favorable compared to the high temperature R phase. We have shown that the R phase is a metal, whereas the M$_1$ phase is found to be an insulator with finite band gap value. Moreover, we numerically demonstrate that a gap can be opened up as the V-V dimer length is varied without incorporating electronic correlations. Hence, our results strongly suggest that the M$_1$ phase is not a conventional Mott insulator given the sensitivity to the dimer distance to its electronic phase. The phonon softening related to the R phase and the phonon stiffening of the M$_1$ phase explain the structural phase transition from the R phase to M$_1$ as temperature is lowered. The V-V dimer has significant impact on both the electronic and vibrational properties of the M$_1$ phase. We show that
the vibrational density of states significantly changes with the variation of the V-V dimer distance. Our calculated vibrational spectra are corroborated by previous neutron scattering experiment as well as our Raman experiment. In particular, our non-spin-polarized calculations of bulk VO$_2$ enable us to gain insight into the structural properties of strained VO$_2$ as found in our Raman experiment.

In addition, we have also performed spin-polarized calculations of both the Rutile and M$_1$ phases of VO$_2$. Our calculations reveal that the AFM-M$_1$ is energetically stable over the AFM-R phase. Both the FM-M$_1$ and FM-R phases of VO$_2$ are found to be almost the same in energy and predicted to be half-metals. The AFM-M$_1$ is found to be insulating, whereas the AFM-R phase is predicted to be appropriate metal. Again, such AFM-M$_1$ phase is also demonstrated to be dynamically stable. On the contrary, the FM-M$_1$ phase is shown to be dynamically unstable. Overall, our work suggests that the SCAN can be utilized for investigating phonon properties of related materials and such work is in progress.

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**APPENDIX A: CONVERGENCE TEST OF OUR LDA RESULTS**

We have checked convergence of our results obtained from the LDA against increasing K mesh as well as energy cut off. As shown in Fig. 18 (top), we have performed calculations for various values of energy cutoff ($E_{\text{cut}}$) ranging from 400 to

![FIG. 18. Convergence of our LDA results against K-mesh and energy cutoff ($E_{\text{cut}}$).](image1)

![FIG. 19. Calculated phonon density of states for the M$_1$ phase of VO$_2$ using the SCAN meta-GGA functional considering ferromagnetic (FM) and antiferromagnetic (AFM) spin ordering.](image2)
APPENDIX B: SPIN-POLARIZED PHONON CALCULATIONS FOR THE M1 PHASE

We have computed the phonon density of states of both the AFM-M1 and FM-M1 phases of VO2 (see Fig. 19). We do not observe negative frequencies in our calculated phonon density of states for the AFM-M1. The absence of any negative frequencies indicates the dynamical stability of the AFM-M1 phase. Moreover, our calculations also suggest that FM-M1 is not dynamical stable.


