I. INTRODUCTION

Transition metal oxides have been widely studied over the past three decades owing to their unprecedented variety of electronic and magnetic properties including high temperature and unconventional superconductivity, complex magnetic orders, and correlated topological phases of matter. In particular, iridates have been proposed as a promising family of materials which could host a number of these phases. Here we report the existence of Dirac nodal lines in the binary oxide IrO$_2$, through a combination of reactive oxide molecular beam epitaxy and angle-resolved photoemission spectroscopy. Unlike in other such materials reported to date, these Dirac nodal lines have the unique property of being simultaneously (i) robust against spin-orbit coupling, as they are protected by the nonsymmorphic symmetry of the rutile structure, and (ii) only partially occupied, since they cross the Fermi level. This should have direct implications on the low-energy physics properties tied to the band velocity such as magnetoresistance and spin Hall effect.

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between 5 and 20 nm were grown at 300 °C in a background pressure of $1 \times 10^{-6}$ distilled ozone. Immediately after growth a single monolayer of crystalline TiO$_2$ ($\sim$1.5 Å) was deposited as a protective cap under the same conditions. Samples were transported in low vacuum and annealed at 350 °C in $2 \times 10^{-5}$ Torr of 10% ozone prior to measurement. This process removes adsorbed contaminants from the surface, but does not remove the TiO$_2$ cap, as demonstrated by the post annealing x-ray photoemission spectroscopy (XPS) data shown in Fig. S3. The XPS Ti 2p signal is expected to originate from the overlayer only since all samples had a thickness of at least 5 nm, much larger than the inelastic mean free path of electrons at a kinetic energy of 600 eV [19]. Note that since TiO$_2$ has a wide band gap [20,21] we do not expect to see in photoemission any contribution from the overlayer in the vicinity of the Fermi level. Further details on the film growth and characterization are available in the Supplemental Material [22].

ARPES measurements over the full three-dimensional (3D) Brillouin zone (BZ) were undertaken at the MAESTRO beamline at the Advanced Light Source using a photon energy of 84–140 eV, with a combined resolution of 15 to 25 meV depending on the photon energy, at temperatures of approximately 70 K. For the experimental geometry see Fig. S5 in Ref. [22].

**B. DFT calculations**

Nonmagnetic DFT calculations were performed using the Quantum ESPRESSO software package [23] using fully relativistic, norm-conserving pseudopotentials for Ir and O [24]. We represented the Kohn-Sham wave functions in a basis set of plane waves extending up to a kinetic energy cutoff of 80 Ry, and used a cutoff of 320 Ry for representing the charge density. An 8 $\times$ 8 $\times$ 12 $k$ mesh was used for Brillouin zone integrations along with Gaussian smearing for band occupations. Perdew-Burke-Ernzerhof parametrization of the generalized gradient approximation (GGA) was employed as the exchange-correlation functional [25]. To ensure that our calculations accurately capture the effects of sizable spin-orbit coupling inherent to iridates, we cross-checked these results against those computed using the full-potential (linearized augmented plane wave plus local orbitals) WIEN2k code [26] and observed negligible differences in the band energies near the Fermi level. After obtaining self-consistent Kohn-Sham eigenstates via DFT, we used the Pw2wannier and Wannier90 codes [27] to construct 20 Wannier functions spanning the manifold of eigenstates surrounding $E_F$ (ten $d$ orbitals per Ir atom times two Ir atoms per unit cell).

**II. METHODS**

**A. Film growth, characterization, and ARPES measurements**

This study is a combination of reactive oxide molecular-beam epitaxy (MBE) synthesis and ARPES. In order to reveal the nodal lines along multiple directions in the reciprocal space, thin films were grown on different surfaces. Epitaxial (110) and (001) oriented IrO$_2$ films were grown on single-crystal TiO$_2$(110) and (001) substrates respectively [see Fig. 1(b) for an x-ray diffraction Cu $K\alpha$ $\theta$/$2\theta$ scan, demonstrating high crystalline quality of both films]. Samples

**III. RESULTS**

**A. Crystal symmetry and electronic structure**

Figure 1(c) shows the band structure along selected high symmetry directions, as obtained by DFT in the GGA approximation including SOC. The results are consistent with the band structure published in Refs. [17,28]. Along A-M and X-M the dispersion consists of a single curve, where for space group No. 136 a nonsymmorphic term adds an additional symmetry to the usual time and space inversions, and as a
FIG. 2. (a) 3D rendering of the calculated Fermi surface, with holelike bands in red and electronlike bands in blue. The gray planes correspond to the BZ center and BZ boundary for the [110] and [001] orientations, and indicate the location of the Fermi surfaces measured by ARPES in (c)–(f), as shown in the insets. (b) The 3D BZ with high symmetry directions hosting the DNLs object of this study, shown in green for the $A$–$M$ line and orange for the $X$–$M$ line. The energy of the band along the $k$ path is color coded as shown. The photon energies used are (c) 124 eV, (d) 84 eV, (e) 140 eV, and (f) 100 eV, and the inner potential $V_0$ used is 11.5 eV for (110) and 4 eV for (001) films, respectively. The sample temperature was $\sim 70$ K. On the left half of (c)–(f), the calculated Fermi surfaces are shown with a $k_z$ broadening of 0.2 Å$^{-1}$. For bulk IrO$_2$, $\pi/a = \pi/b \simeq 0.70$ Å$^{-1}$, $\pi/c \simeq 1.00$ Å$^{-1}$. The experimental data show a slight mismatch with the drawn bulk BZs in view of the strain on films. In all ARPES plots and in the text we name $xy$ the sample surface plane and $z$ the axis normal, for both orientations. As a consequence, $k_z$ is the out of plane momentum regardless of the surface.

consequence the band degeneracy increases from double to fourfold. Namely, the combination of a translation of half the body diagonal $\tau$ and a fourfold rotational symmetry around the $c$ axis provides the degeneracy along $A$–$M$ [Fig. 1(d)], while the combination of $\tau$ and mirror symmetry with respect to the $a$ axis is responsible for that along $X$–$M$ [Fig. 1(e)].

B. Comparison to DFT

The choice of the sample orientation for measuring the DNLs is in principle arbitrary, but because of the strong photon energy dependence of the photoemission intensity in IrO$_2$ we choose to measure $A$–$M$ on the (110) surface and $X$–$M$ on the (001) surface, respectively, where they can be followed at constant $h\nu$.

The calculated 3D Fermi surface is shown in Fig. 2(a), and consists of two sheets of holelike states (red) and one of electronlike states (blue). The reciprocal space locations of the nodal lines are shown in Fig. 2(b), with the $A$–$M$ line in green and the $X$–$M$ line in orange, the latter forming closed loops. It is apparent that the $A$–$M$ line is more naturally accessible by ARPES on the (110) surface, as the whole line can be measured at a single photon energy, while the $X$–$M$ line is more easily measured on the (001) surface. This motivates the synthesis and measurement of these two orientations of IrO$_2$. In Figs. 2(c) and 2(d) and Figs. 2(e) and 2(f) we show the measured Fermi surfaces for (110) and (001) films, respectively, at the center [Figs. 2(c) and 2(e)] and at the boundary [Figs. 2(d) and 2(f)] of the BZ, compared to simulated Fermi surface maps from DFT with an added $k_z$ broadening of 0.2 Å$^{-1}$. Aside from a slight discrepancy between the relative sizes of the hole and electron pockets in the (110) surface, the experimental results match with the DFT predictions, with no observable surface states as opposed to what previously claimed [29] (this point is further clarified in Fig. S4). Considering the importance of correlations in partially filled $d$ orbitals, it is not a priori guaranteed that a DFT approach is a good starting point, and therefore the presence of such agreement is not a trivial observation.
The results shown in Figs. 2(c) and 2(d) are consistent with earlier ARPES measurements on IrO$_2$(110) [28,29], though the present data are the most extensive to date and the first ones on IrO$_2$(001). In regards to these constant energy maps, it is worthwhile to note that the ARPES intensity is fairly isotropic with $p$ polarization, but shows a clear suppression in $s$ polarization along the $k_y$ and $k_z$ axes, as we show in Fig. S5 for the Fermi surface measured on (110) at the $M$ point. This is immediate consequence of some degree of orbital ordering in IrO$_2$ [30], as opposed to the perovskite iridates where the orbital momentum $L$ is not a good quantum number and ARPES shows no dipole matrix element effects [10]. The minor role of correlations in IrO$_2$ in comparison with other iridates is believed to stem from the different arrangement and higher connectivity of the octahedra in the rutile structure [28,30].

C. Evolution of the nodal lines

In Fig. 3 we focus more directly on the measurement of the nodal lines, starting from the $A$-$M$ direction in the (110) sample. In Fig. 3(a) the Fermi surface of Fig. 2(c) is inserted in the 3D BZ. The dashed lines mark the locations of the $E$ vs $k_z$ images (with $k_y$ normal to the plane containing the DNL) shown in Figs. 3(b)–3(g), in direction of $M$ to $A$ as indicated by the arrow. The ensuing nodal line dispersion is shown in the $E$ vs $k_z$ image of Fig. 3(h). The DFT bands are superposed to the data for clarity. Near $M$ the electronic states are unoccupied as the Fermi surface consists of a hole pocket. Taking cuts in direction of $A$, the crossing point moves to and below the Fermi level. The band dispersion in the vicinity of the crossing point becomes less clear towards $A$ where it is further from the Fermi level. Because of the aforementioned underestimation of the hole pockets, the theory agrees with the data but with a mismatch in the binding energy of the crossing point (the mismatch is large enough that the Fermi level crossing of the Dirac node in DFT is outside the range shown here for the $A$-$M$ line). Figures 3(j)–3(o) are the counterparts of the top panels, now for the $X$-$M$ line, with the Fermi surface from Fig. 2(e) inserted in Fig. 3(i). The Fermi surface is slightly electronlike at $X$, with a crossing point at $\sim 50$ meV binding energy, and evolves into the holelike sheet at $M$. The nodal line dispersion is shown Fig. 3(p). The band dispersion at the crossing points is not guaranteed to be linear over a large energy range, and while in some cases a roughly linear dispersion extends over more than 1 eV [31], in others the dispersion has a higher order term at all energies [32].

In IrO$_2$ the linear dispersion is clearly visible over several hundreds of meV only along $X$-$M$, while along $A$-$M$ the bands appear parabolic all the way to the crossing point. Within the limitations dictated by the experimental broadening of the linewidth, we cannot find the presence of any gap in either nodal line. Also the dispersion along $R$-$A$-$R$ measured on the (001) surface, where the dispersion can be more easily followed, clearly hints at a gapless crossing at $A$ (see Fig. S6). On this point, note that, as opposed to the many instances of quasi 2D materials hosting Dirac crossings, more sophisticated analysis methods aiming to exclude the presence of a gap in bulk states of 3D systems do not seem, in general, justified. Due to the finite escape depth of photoelectrons, ARPES data present an intrinsic $k_z$ broadening. Using a reasonable value of $\lambda = 5$ Å for the electron mean free path, we obtain an approximate $k_z$ distribution over $1/\lambda = 0.2$ Å$^{-1}$ [33]. For IrO$_2$, along both nodal lines, at a $k_z$ value 0.1 Å$^{-1}$ away from the Dirac node, a gap larger than 50 meV is expected (see Fig. S7). The strict identification of a crossing point in bulk states is therefore not possible, and the presence of a single peak depends on the exact $k_z$ dispersion.

FIG. 3. (a) The Fermi surface for the (110) surface at the BZ center, from Fig. 2(b). The dashed lines and the arrow indicate the locations of the dispersion images for the data in (b)–(g), where the DFT results are superposed as dashed curves, (i) and (j)–(o) The equivalent of (a) and (b)–(g) for the (001) surface. (h) and (p) The nodal line dispersion along $A$-$M$-$A$ and $X$-$M$-$X$, respectively. The sample temperature was $\sim 70$ K. The photon energy is 124 eV for $A$-$M$ and 140 eV for $X$-$M$. 
in the vicinity of the node and on other (extrinsic) broadening factors. In addition to the above, whereas growth on the (001) surface preserves the space group symmetry, in (110) films the surface epitaxial strain distorts the rutile structure, breaking the symmetry terms which protect the nodal lines. For a unit cell distortion by \( \sim 2\% \) along [110], \( \sim -5\% \) along [001], and \( \sim 0.8\% \) along [110] (normal to the surface plane), as inferred by x-ray diffraction (see Ref. [22]), DFT predicts an opening of a gap as large as \( \sim 50 \) meV depending on the parallel momentum, as shown in Fig. 59.

### IV. DISCUSSION

There is an apparent difference between the electronic structure of IrO\(_2\) and that of the other DNL materials reported so far. Both nodal lines here have a large energy dispersion \( (\sim 0.5 \text{ eV}) \) and they cross the Fermi level, making it a unique case. As an immediate consequence, any contribution to the low energy physics can be expected to be robust against perturbations which shift the chemical potential.

Nodal lines may be categorized on the basis of which symmetry terms are at their origin, with some compounds believed to host more than a single type. When time-reversal symmetry is required for its existence, by definition the nodal line is not robust against SOC. The lifting of the degeneracy can be minor in materials with a small spin-orbit term [34–36], but dramatic in those containing heavy elements [37,38]. Protection from SOC requires an additional symmetry other than space inversion, namely a nonsymmorphic term in the crystal space group [18] (a separate case is the one of Weyl nodal lines, which are protected by mirror symmetry and where the spin components are split by broken time or space inversion symmetry [39]). The accepted examples of DNLs protected by nonsymmorphic symmetry are mostly found in crystals of the \( P4/\text{mmm} \), No. 129 space group, namely the family of Zr(Hf)SiX compounds (X=S, Se, Te) [31,40–42] and InBi [43], whereas IrO\(_2\) crystallizes in space group No. 136. A number of others have been predicted [44,45] but not yet experimentally verified.

In contrast to IrO\(_2\), however, both in InBi and in the Zr(Hf)SiS family the nonsymmorphic symmetry protected DNL along \( X-R \) is far below the Fermi level, making it out of reach for low energy excitations [43,46]. The nodal lines lying on the natural (001) cleaving plane, on the other hand, show a small dispersion along the characteristic diamond-shaped Fermi surface and are unstable against SOC, with a gap opening from \( \sim 20 \) meV to several tens of meV depending on the spin-orbit term of the atomic species in the crystal. In ZrSiTe the \( X-R \) line is instead believed by theory to lie much closer to the Fermi level, but it could not be seen in experiments, possibly because of natural hole doping in this family of layered crystals [42].

A separate mention deserves the case of RuO\(_2\), which is isostructural to IrO\(_2\) and was recently found to host a nodal line along the \( X-R \) high symmetry direction, crossing the Fermi level [47]. Although there is no symmetry protection along \( X-R \), the small SOC of Ru \( (\sim 0.13 \text{ vs. } \sim 0.41 \text{ eV}) \) relative to Ir [48], together with the obligated fourfold degeneracy at \( X \), makes it so that the gap is only a few meV in the vicinity of \( X \), where the Fermi level crossing occurs. This provides a useful term of comparison between a material with low energy states consisting of a DNL strictly protected against SOC, and one with a very similar band structure but with lifted degeneracy, albeit by a small gap. How much influence such perturbation may have on the low energy properties is an open question, and it is argued by several authors that in materials with light elements the effect of SOC on the DNL could be considered in practice negligible [34,36].

The comparison is particularly relevant between IrO\(_2\) and RuO\(_2\) since the two are widely studied in electrochemistry for water splitting. In RuO\(_2\)(110) a surface state pinned to the nodal line was observed, but its role for photocatalysis remains uncertain since IrO\(_2\) shows a similar activity ratio [49] but does not host any surface state. Also, the influence on chemistry of the details of the band structure at a given orientation seems difficult to reconcile with the higher efficiency reported in amorphous compared to rutile RuO\(_2\) films [50].

IrO\(_2\) was shown to exhibit large magnetoresistance [51,52], for which a key quantity is the electron mobility, and therefore the band velocity. It is difficult to infer a reliable Fermi velocity for the \( A-M \) DNL where the carriers are massive except for a small region around the crossing point. In contrast, the band velocity in the \( X-M \) DNL along the \( \Gamma-X \) direction is linear over a large range [Fig. 3(j)], and we extract \( h v_F \leq 3.1 \text{ eV } \AA \), a large value, higher than \( \sim 2 \text{ eV } \AA \) in RuO\(_2\) [47], comparable to \( \sim 3-5 \text{ eV } \AA \) for the Dirac crossing at \( X \) in Zr(Hf)SIS [31,42] and about half of \( \sim 6.5 \text{ eV } \AA \) in graphene [53]. These considerations altogether hint at the possibility that IrO\(_2\) may be a viable candidate for magnetoresistive devices. However, the large variations observed within the different DNL compounds—the magnetoresistance in IrO\(_2\) [51,52] is larger than in good conductors such as noble or alkali metals [54], but at least two orders of magnitude smaller than in ZrSiS [55,56], and at least three orders of magnitude smaller than in the WP\(_2\) and MoP\(_2\) Weyl semimetals [54], all layered, quasi-2D compounds—clearly indicates that the presence of massless fermions is not linked to the magnetotransport properties in a straightforward way and is instead strongly dependent on the fermiology of the material.

This work has shown that the binary oxide IrO\(_2\) has an exotic electronic structure consisting of a network of intersecting nodal lines along \( A-M \) and \( X-M \) where the band crossings are protected by nonsymmorphic symmetry against strong SOC. These nodal lines are unusual in that they disperse strongly in energy and cross the Fermi level. Some aspects make IrO\(_2\) a nontrivial target for further work aiming to tune and explore new topological properties. The rutile structure is more three dimensional and therefore (i) has a more complex fermiology, and (ii) is less prone to modular heterostructuring where electronic properties can be altered and engineered with strain and confinement, with respect to layered compounds such as perovskites. In view of studying the interplay of SOC-driven topological phases and correlations [6], it lies in the weak correlation limit due to the large (\( \sim 3 \text{ eV} \)) bandwidth of its \( t_{2g} \) states. Nonetheless, aside from the important differences established above with respect to the DNL compounds discovered so far, IrO\(_2\) is an exciting playground for this field in that it is a simple binary transition metal oxide, already widely

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